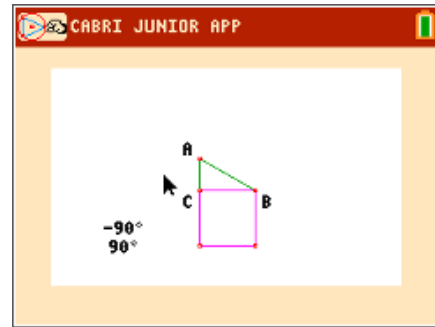




### Problem 1 – Squares on Sides Proof

1. Why is the constructed quadrilateral a square?



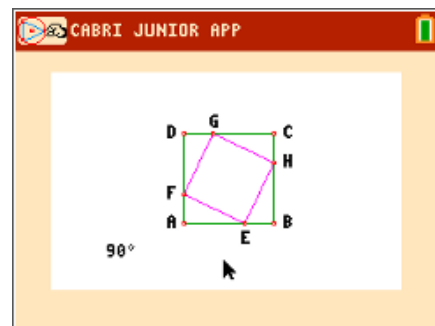
2. Record three sets of area measurements you made by dragging points  $A$ ,  $B$ , and/or  $C$ .

Square on $\overline{BC}$	Square on $\overline{AC}$	Sum of squares	Square on $\overline{AB}$

3. What conjecture can you make about the areas of the three squares? Does this relationship always hold when a vertex of  $\triangle ABC$  is dragged to a different location?

### Problem 2 – Inside a Square Proof

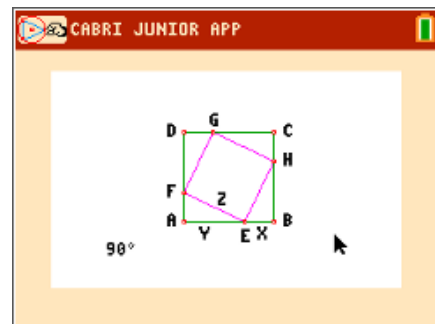
4. Prove that constructed quadrilateral  $EFGH$  is a square.



5.  $ABCD$  is a square with all sides of length  $(x + y)$ .

The area of the square  $ABCD$  is  $(x + y)^2 = x^2 + 2xy + y^2$

Each of the triangles,  $\triangle EFA$ ,  $\triangle FGD$ ,  $\triangle GHC$  and  $\triangle HEB$ , is a right triangle with height  $x$  and base  $y$ . So, the area of each triangle is  $\frac{1}{2}xy$ .





# The Pythagorean Theorem

## Student Activity

Name \_\_\_\_\_

Class \_\_\_\_\_

$EFGH$  is a square with sides of length  $z$ . So the area of  $EFGH$  is  $z^2$ .

Looking at the areas in the diagram we can conclude that:

$$ABCD = \triangle EFA + \triangle FGD + \triangle GHC + \triangle HEB + EFGH$$

Substitute the area expressions (with variables  $x$ ,  $y$ , and  $z$ ) into the equation above and simplify.

6. Record three sets of numeric values for  $\triangle HEB$ .

$BE$	$BE^2$	$HB$	$HB^2$	$BE^2 + HB^2$	$EH$	$EH^2$

7. Does  $BE^2 + HB^2 = EH^2$  when  $E$  is dragged to a different location?
8. Does  $BE^2 + HB^2 = EH^2$  when  $A$  or  $B$  is dragged to a different location?