

# Circular Functions Test 3A

Name: \_\_\_\_\_

7 8 9 10 11 12



Navigator



Assessment



Student



30 min

## Question: 1

If  $\sec(x) = 3$  and  $\frac{3\pi}{2} \leq x \leq 2\pi$ , then  $\sin(x)$  is equal to:

- a)  $-\frac{\sqrt{3}}{2}$       b)  $\frac{\sqrt{3}}{2}$       c)  $\frac{1}{3}$       d)  $-\frac{2\sqrt{2}}{3}$       e)  $\frac{2\sqrt{2}}{3}$

## Question: 2

If  $\cot(\alpha) = 1 + \frac{1}{x}$  and  $0 \leq \alpha \leq \frac{\pi}{2}$ , then  $\cos^2(\alpha)$  is equal to:

- a)  $\frac{x^2 + 2x + 1}{2x^2 + 2x + 1}$       b)  $\frac{x^2}{2x^2 + 2x + 1}$       c)  $\frac{x}{\sqrt{2x^2 + 2x + 1}}$       d)  $\frac{x + 1}{\sqrt{2x^2 + 2x + 1}}$       e)  $\frac{1}{x^2}$

## Question: 3

If  $\sin(\alpha) = \frac{3}{5}$  and  $0 \leq \alpha \leq \frac{\pi}{2}$ , then  $\sin(2\alpha)$  is equal to:

- a)  $\frac{6}{5}$       b)  $\frac{3}{10}$       c)  $\frac{12}{25}$       d)  $\frac{24}{25}$       e)  $\frac{7}{25}$

## Question: 4

If  $\sin(\alpha) = \frac{3}{5}$  and  $\cos(\beta) = \frac{12}{13}$  where  $\alpha \in \left[0, \frac{\pi}{2}\right)$  and  $\beta \in \left[0, \frac{\pi}{2}\right)$  then  $\cos(\alpha - \beta)$  is equal to:

- a)  $-\frac{8}{65}$       b)  $\frac{16}{65}$       c)  $\frac{33}{65}$       d)  $\frac{63}{65}$       e)  $\frac{62}{65}$

## Question: 5

If  $\sec(\alpha) = x$  and  $\alpha \in \left(0, \frac{\pi}{2}\right)$  and  $\sec(\beta) = x$  where  $\beta \in \left(\frac{3\pi}{2}, \frac{5\pi}{2}\right)$  then  $\beta$  in terms of  $\alpha$  is:

- a)  $2\pi + \alpha$       b)  $2\pi - \alpha$       c)  $2\pi \pm \alpha$       d)  $\pi + \alpha$       e)  $\pi \pm \alpha$

## Question: 6

Given  $y > x > 0$  then  $\tan\left(\sin^{-1}\left(\frac{x}{y}\right)\right)$  is equal to:

- a)  $\frac{y}{\sqrt{x^2 - y^2}}$       b)  $\frac{x}{\sqrt{y^2 - x^2}}$       c)  $\frac{x}{y - x}$       d)  $\frac{\sqrt{y^2 - x^2}}{x}$       e)  $\frac{\sqrt{y^2 - x^2}}{y}$

**Question: 7**

Given  $0 \leq x \leq 1$  then  $\sin\left(\sin^{-1}(x) + \sin^{-1}\left(\sqrt{1-x^2}\right)\right)$  is equal to:

- a)  $\frac{\pi}{2}$                       b)  $\pi$                       c) 0                      d) -1                      e) 1

**Question: 8**

The graph of  $y = \tan^{-1}\left(\frac{x}{2}\right)$  has asymptotes at:

- a)  $y = -2$  and  $y = 2$                       b)  $x = -2$  and  $x = 2$   
 c)  $y = -\frac{\pi}{2}$  and  $y = \frac{\pi}{2}$                       d)  $x = -\frac{\pi}{2}$  and  $x = \frac{\pi}{2}$   
 e)  $y = -\pi$  and  $y = \pi$

**Question: 9**

Given the function defined by the rule:  $f(x) = a + b \sin^{-1}(cx)$  where  $a$ ,  $b$  and  $c$  are real, non-zero constants, then the maximal domain of  $f(x)$  is:

- a)  $[-c, c]$                       b)  $\left[-\frac{a}{b}, \frac{a}{b}\right]$   
 c)  $\left[\frac{c(a-1)}{b}, \frac{c(1-a)}{b}\right]$                       d)  $\left[-\frac{1}{c}, \frac{1}{c}\right]$   
 e)  $\left[-\frac{\pi}{2c}, \frac{\pi}{2c}\right]$

**Question: 10**

Given the function defined by the rule:  $f(x) = a + b \tan^{-1}(c(x-d))$  where  $a$ ,  $b$ ,  $c$  and  $d$  are real positive constants, then the range of  $f(x)$  is:

- a)  $[a-b, a+b]$                       b)  $(-\infty, \infty)$   
 c)  $[a-b\pi, a+b\pi]$                       d)  $\left(a - \frac{b\pi}{c}, a + \frac{b\pi}{c}\right)$   
 e)  $\left(a - \frac{b\pi}{2}, a + \frac{b\pi}{2}\right)$